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# The Yb<sub>2</sub>Al<sub>1-x</sub>Mg<sub>x</sub>Si<sub>2</sub> series from a spin fluctuation (x = 0) to a magnetically ordered ground state (x = 1)

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# Abstract

The structural and magnetic properties of Yb<sub>2</sub>Al<sub>1-x</sub>Mg<sub>x</sub>Si<sub>2</sub> (x = 0, 0.5 and 1), crystallizing in the tetragonal Mo<sub>2</sub>FeB<sub>2</sub>-type structure, are reported in this work. Yb<sub>2</sub>AlSi<sub>2</sub> exhibits a Pauli paramagnetic ground state arising due to spin/valence fluctuations induced by a significant Yb 4f conduction band hybridization. High-field magnetization (up to 120 kOe) indicates a nearly temperature-independent susceptibility of  $8.6 \times 10^{-3}$  emu/Yb mol below 10 K. On the other hand, Yb ions in Yb<sub>2</sub>MgSi<sub>2</sub> order antiferromagnetically at a relatively high temperature  $T_N$  of 9.5 K. The intermediate composition alloy Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub> is a Kondo lattice, antiferromagnet with  $T_N = 5.5$  K. The coefficient of the linear term of the electronic heat capacity,  $\gamma$ , of Yb<sub>2</sub>AlSi<sub>2</sub> is found to be 305 mJ mol<sup>-1</sup> K<sup>-2</sup>, indicating a significant electronic mass enhancement due to strong electronic correlations. Below 12 K, an additional contribution to the heat capacity of the form  $T^3 \ln T$  is observed. The <sup>170</sup>Yb Mössbauer spectra in the ordered state of Yb<sub>2</sub>MgSi<sub>2</sub> indicate a strong coupling of the 4f quadrupolar moment with the magnetic moment through a magneto-elastic coupling.

(Some figures in this article are in colour only in the electronic version)

# 1. Introduction

Yb<sub>2</sub>AlSi<sub>2</sub> [1] and Yb<sub>2</sub>MgSi<sub>2</sub> [2] are known to form in the tetragonal Mo<sub>2</sub>FeB<sub>2</sub>-type structure with space group P4/mbm, which is a ternary ordered derivative of the U<sub>3</sub>Si<sub>2</sub> structure. In the binary prototype, the uranium ions occupy two distinct lattice sites, 4h and 2a, but in the ternary derivative the Yb ions occupy the unique 4h site of the unit cell. This makes these two Yb compounds attractive for an exploration of their magnetic properties as complexities due to a possible site-dependent magnetic response should be absent. The study of Yb-based compounds is important as it enriches our understanding of the strongly correlated electron behavior in metals, arising from an enhanced interaction between the local Yb 4f moment and the conduction electrons.

 $Yb_2MgSi_2$  is one of the members of a series of isostructural compounds of composition  $R_2MgSi_2$  (R = Y,

La-Nd, Sm, Gd-Lu). The cell volume of Yb<sub>2</sub>MgSi<sub>2</sub> follows the behavior expected on the basis of lanthanide contraction when compared with those of the neighboring analogs and thus suggests a trivalent Hund's-rule-derived  ${}^{2}F_{7/2}$  state of the Yb ions [2, 3]. On the other hand, in the case of  $R_2AlSi_2$  the analogs with R = Y, Ho, Er, Tm and Lu adopt the orthorhombic W2CoB2-type structure and hence the possible magnetic state of the Yb ions in Yb2AlSi2 cannot be ascertained from cell volume considerations [1]. In this report we have carried out a detailed study of the magnetic behavior of these two Yb compounds using the techniques of magnetization, heat capacity, electrical resistivity and <sup>170</sup>Yb Mössbauer spectroscopy. We find that the Yb<sup>3+</sup> ions order magnetically in Yb2MgSi2 at a relatively high temperature of 9.5 K, when compared with the magnetic ordering temperature of nearly 31 K in isostructural Gd<sub>2</sub>MgSi<sub>2</sub>. On the other hand, Yb<sub>2</sub>AlSi<sub>2</sub> exhibits a Pauli paramagnetic, moderate

**Table 1.** Lattice constants as obtained by Guinier powder patterns for the compounds  $Yb_2Al_{1-x}Mg_xSi_2$  (x = 0, 0.5 and 1) and  $Gd_2MgSi_2$  (tetragonal Mo<sub>2</sub>FeB<sub>2</sub> type; tP10, P4/mbm).

		Lattice constants		Unit cell volume
Compound	Heat treatment	a (Å)	<i>c</i> (Å)	$V_{\rm U}$ (Å <sup>3</sup> )
Yb <sub>2</sub> AlSi <sub>2</sub>	900 °C—11 days 800 °C—9 days	6.7731(4)	4.2403(4)	194.52(5)
$\begin{array}{l} Yb_2Al_{0.5}Mg_{0.5}Si_2\\ Yb_2MgSi_2\\ Gd_2MgSi_2 \end{array}$	800 °C—10 days 800 °C—6 days 800 °C—8 days	6.9234(8) 7.0530(6) 7.233(1)	4.1669(6) 4.1282(5) 4.2519(7)	199.30(5) 205.52(8) 221.8(1)

heavy fermion ground state arising from a significant Yb 4f conduction band hybridization. Due to the diametrically opposite nature of the magnetic ground state in these two end members, we also studied  $Yb_2Al_{0.5}Mg_{0.5}Si_2$ , which orders magnetically at 5.5 K and shows Kondo behavior in the temperature variation of its resistivity.

## 2. Experimental details

Due to the high vapor pressure of Yb and Mg metal, Yb<sub>2</sub>AlSi<sub>2</sub>, Yb<sub>2</sub>MgSi<sub>2</sub>, Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub> and Gd<sub>2</sub>MgSi<sub>2</sub> were prepared in sealed, degassed tantalum crucibles. The metals used were commercial products with high purity (99.9 wt% for the rare earths; 99.99 wt% for aluminum and magnesium; 99.999 wt% for silicon). Weighed amounts of the elements (small pieces for Yb and turnings for Gd freshly prepared from surfacecleaned ingots; Mg and Al in the form of chips and turnings, respectively; fine grains for Si) with a total mass of about 2 g were directly set and slightly pressed together into out-gassed tantalum crucibles; they were sealed by arc welding under a flow of pure argon. Samples were melted by slowly heating the crucibles in a high-frequency induction furnace and the crucibles shaken to ensure homogenization; this procedure was repeated twice. The crucibles were then sealed under vacuum in guartz tubes and annealed in resistance furnaces; the details of the heat treatment are given in table 1. No contamination of the alloys due to reactivity towards the container material (Ta) was noticed.

X-ray analysis was carried out by means of powder diffraction methods; powder patterns were obtained by a Guinier–Stoe camera using Cu K $\alpha$  radiation ( $\lambda = 1.5418$  Å) and pure Si as an internal standard (a = 5.4308 Å); the Guinier patterns were indexed with the help of the LAZY-PULVERIX program [4] and the lattice parameters determined by the least-squares methods. Metallographic specimens were prepared by the standard polishing methods of a fragment cut from the bulk samples. Magnetization as a function of temperature and applied magnetic field was measured with a superconducting quantum interference device (Quantum Design) and vibrating sample magnetometers (Oxford Instruments). The heat capacity and electrical resistivity were measured in a physical property measuring system (Quantum Design). <sup>170</sup>Yb Mössbauer measurements  $(E_0 = 84.3 \text{ keV}, I_g = 0, I_e = 2)$  were performed with a TmB<sub>12</sub>  $\gamma$ -ray source mounted on an electromagnet drive with triangular velocity signal (1 mm s<sup>-1</sup> = 68 MHz).



Figure 1. The x-ray powder diffraction patterns of  $Yb_2MgSi_2$  and  $Yb_2AlSi_2$ .

### 3. Results and discussion

#### 3.1. Structure

X-ray powder diffraction patterns of  $Yb_2AlSi_2$  and  $Yb_2MgSi_2$ are shown in figure 1. All the peaks can be indexed to the tetragonal Mo<sub>2</sub>FeB<sub>2</sub>-type symmetry, showing that the samples are single phase. This is further confirmed by metallographic analysis. In the Gd sample an extra parasitic phase (about 6%), whose exact composition was not determined, was present.

Crystallographic data and lattice constant values of the various compounds are reported in table 1. For  $Yb_2Al_{1-x}Mg_xSi_2$  (x = 0, 0.5 and 1), the increase of the unit cell volume (which is nearly linear) in passing from the Al ( $V_{\rm U} = 194.52(5)$  Å<sup>3</sup>) to the Mg compound ( $V_{\rm U} =$ 205.52(8) Å<sup>3</sup>) is expected taking into account the atomic volumes of the elements. It may be noted that the expansion is not isotropic and that the two lattice parameters of the tetragonal Mo<sub>2</sub>FeB<sub>2</sub>-type unit cell follow opposite trends: the a axis undergoes an expansion while the c axis shows a slight contraction. The near-neighbor atoms of Yb in Yb2AlSi2 are 2 Si at 2.845 and 4 Si at 2.956 Å, respectively, followed by 4 Al at 3.267 Å [1]. Therefore, the Yb–Si ligand interaction may be the dominant factor in determining the hybridization experienced by the Yb 4f electronic wavefunctions in these compounds. Al (and Mg) being at the third-nearest-neighbor distance may primarily affect the electronic band structure by the number of valence electrons donated to the conduction band and by their size on the unit cell volume.

#### 3.2. Magnetization

Figure 2 shows the inverse susceptibility  $\chi^{-1}$  of Yb<sub>2</sub>MgSi<sub>2</sub> versus temperature between 1.8 and 300 K in an applied field of 2 kOe. The data present an almost perfect Curie–Weiss law between 300 and 10 K, with the effective moment  $\mu_{eff}$  of 4.54  $\mu_{\rm B}$  appropriate for Yb<sup>3+</sup> and a paramagnetic Curie temperature  $\theta_{\rm p} = -35$  K indicative of antiferromagnetic (AF) interactions. The peak at  $T_{\rm N} = 9.5$  K (upper inset, figure 2) signifies the onset of magnetic ordering of the Yb<sup>3+</sup> moments,



**Figure 2.** The inverse susceptibility  $\chi^{-1}$  of Yb<sub>2</sub>MgSi<sub>2</sub> between 1.8 and 300 K. The solid line is a fit of the Curie–Weiss law to the data. The upper inset shows  $\chi$  below 20 K;  $T_N$  is indicated by an arrow. The lower inset depicts the in-field magnetization up to 70 kOe at 1.8 K.

probably with an AF structure. The large value of the ratio  $|\theta_p|/T_N \sim 3.5$  points either to the importance of next-nearestneighbor exchange or to the presence of 4f conduction electron hybridization. The isothermal magnetization at 1.8 K is linear with the field and furnishes a magnetization of nearly 1.5  $\mu_B$ per formula unit at the highest applied field of 70 kOe. The variation of the magnetization with field is in conformity with the AF nature of the magnetic transition at 9.5 K.

The magnetic behavior of Yb2AlSi2 as probed by magnetization is different. Figure 3 shows  $\chi$  and  $\chi^{-1}$  between 1.8 and 300 K. The susceptibility increases monotonically with decreasing temperature, attaining a value of  $\sim 17 \times$  $10^{-3}$  emu/Yb mol at the lowest temperature of 1.8 K. There is no signature of a magnetic transition and the magnetic response in Yb<sub>2</sub>AlSi<sub>2</sub> is considerably weaker than in Yb<sub>2</sub>MgSi<sub>2</sub>. For example,  $\chi$  of Yb<sub>2</sub>MgSi<sub>2</sub> at 15 K in the paramagnetic state is 57  $\times$  10<sup>-3</sup> emu/Yb mol compared to the corresponding value of  $11.2 \times 10^{-3}$  emu/Yb mol in Yb<sub>2</sub>AlSi<sub>2</sub>. Between 200 and 300 K,  $\chi^{-1}$  of Yb<sub>2</sub>AlSi<sub>2</sub> follows nearly a Curie-Weiss behavior with  $\mu_{\rm eff} = 4.2 \ \mu_{\rm B}$  and  $\theta_{\rm p} = -203$  K. The large, negative  $\theta_p$  is a characteristic feature of spin/valence fluctuating Yb compounds in which the strong 4f conduction electron hybridization destabilizes the 4f-derived local moment and gives rise to a Pauli paramagnetic ground state. The weak monotonic increase of the susceptibility at low temperatures in Yb<sub>2</sub>AlSi<sub>2</sub> may or may not be intrinsic. In the latter case, Curielike 'tails' override the temperature-independent susceptibility at low temperatures due to the presence of a tiny fraction of Yb ions in a trivalent electronic state due to the proximity of defects, site exchange, impurities or minor parasitic magnetic phases. Isothermal magnetization was measured up to 120 kOe



**Figure 3.** The susceptibility  $\chi$  and inverse susceptibility  $\chi^{-1}$  of Yb<sub>2</sub>AlSi<sub>2</sub> between 1.8 and 300 K. The solid line is a fit of the Curie–Weiss law to the data. The filled black circles show the likely intrinsic  $\chi$  of Yb<sub>2</sub>AlSi<sub>2</sub> (see the text).



**Figure 4.** The in-field magnetization of  $Yb_2AlSi_2$  up to 120 kOe at 2, 5 and 10 K. The solid line is a linear fit to the data between 80 and 120 kOe taken at 5 K.

at 2, 5 and 10 K to probe the variation of the magnetization with field and the data are shown in figure 4. There is a slight curvature in the magnetization at low fields but at higher fields, i.e. above  $\sim 70$  kOe, a linear response is noted. From the linear portion of the in-field magnetization between 80 and 120 kOe we obtain  $\chi$  values of 8.54  $\times$  10<sup>-3</sup>, 8.6  $\times$  10<sup>-3</sup> and 8.65  $\times$  10<sup>-3</sup> emu/Yb mol, respectively, at 2, 5 and 10 K. Thus, the high-field magnetization data suggest that the intrinsic susceptibility of Yb2AlSi2 is nearly temperatureindependent at least below 10 K. Subtracting a constant term of  $8.6 \times 10^{-3}$  emu/Yb mol from the susceptibility data below 10 K of Yb<sub>2</sub>AlSi<sub>2</sub>, the remaining contribution is accounted for well by a Curie–Weiss description with Curie constant  $C_{CW}$  of 0.0354 emu mol<sup>-1</sup> K<sup>-1</sup> and  $\theta_p = -2.2$  K. If it is assumed that this (extrinsic) contribution is due to Yb3+ ions alone, it implies a presence of about 1.5% of trivalent Yb in the sample. The filled black circles in figure 3 show the susceptibility obtained after the contribution calculated from the values of  $C_{\rm CW}$  and  $\theta_{\rm p}$ is subtracted.

The observation of antiferromagnetic and paramagnetic ground states in the isostructural Yb<sub>2</sub>MgSi<sub>2</sub> and Yb<sub>2</sub>AlSi<sub>2</sub>, respectively, prompted us to probe the magnetic properties at an intermediate composition Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub>. The low-field



**Figure 5.** The inverse susceptibility  $\chi^{-1}$  of Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub> between 1.8 and 300 K. The solid line is a fit of the Curie–Weiss law to the data. The lower inset shows below  $\chi$  15 K;  $T_N$  is indicated by an arrow.

susceptibility taken in an applied field of 50 Oe (lower inset figure 5) shows an AF transition near 5.5 K. The inverse susceptibility measured in a field of 2 kOe, plotted in the main panel, shows Curie–Weiss behavior in an extended range of temperatures similar to Yb<sub>2</sub>MgSi<sub>2</sub> with parameters  $\mu_{eff} = 4.4 \ \mu_B$  and  $\theta_p = -91$  K. While  $\mu_{eff}$  indicates a nearly trivalent state of the Yb ions, which is in conformity with the AF transition at low temperature, a large, negative  $\theta_p$  signifies an enhanced hybridization between Yb 4f and conduction electrons, lying intermediate between Yb<sub>2</sub>AlSi<sub>2</sub> and Yb<sub>2</sub>MgSi<sub>2</sub>.

#### 3.3. Resistivity

The electrical resistivities of Yb<sub>2</sub>AlSi<sub>2</sub>, Yb<sub>2</sub>MgSi<sub>2</sub> and Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub> are shown in figure 6. The resistivity of paramagnetic Yb<sub>2</sub>AlSi<sub>2</sub> shows a slight negative temperature coefficient between 300 and 200 K and drops gradually below 100 K. Qualitatively, similar behavior has been reported in UAl<sub>2</sub> [5], YbCuAl [6] and some other 4f-and 5f-based spin/valence fluctuation compounds. Evidence for spin/valence fluctuations in Yb<sub>2</sub>AlSi<sub>2</sub> due to 4f conduction electron hybridization has been inferred above from the magnetization data. The analysis of the resistivity data at low temperatures reveals that the resistivity follows a quadratic variation (i.e.  $\rho = \rho_0 + AT^2$ ) with  $A = 1.195 \times 10^{-6} \Omega$  cm. The magnitude of A falls in the range observed for various spin fluctuation and heavy fermion compounds [7].

The electrical resistivity of Yb<sub>2</sub>MgSi<sub>2</sub> shows a distinct anomaly at the magnetic transition near 9.5 K. The resistivity decreases rapidly below 9.5 K (see the inset of figure 6(b)) due to the freezing of the spin-disorder-induced scattering of the charge carriers. In the paramagnetic regime the resistivity tends to saturate at high temperatures and qualitatively its thermal variation tends to acquire a character similar to that of Yb<sub>2</sub>AlSi<sub>2</sub>. We have already remarked above that a negative  $\theta_p$ 



**Figure 6.** The electrical resistivity  $\rho$  of (a) Yb<sub>2</sub>AlSi<sub>2</sub>; the inset shows the quadratic variation of  $\rho$  with temperature *T* below 4 K, ((b), (c)) Yb<sub>2</sub>MgSi<sub>2</sub> and Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub>; the arrows in the insets mark the rapid drop in  $\rho$  due to magnetic ordering.

of -35 K in Yb<sub>2</sub>MgSi<sub>2</sub> may imply a tendency of 4f conduction band hybridization-induced spin fluctuations. The thermal variation of resistivity at higher temperatures tends to favor such a conclusion.

The resistivity of the pseudo-ternary alloy Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub> Si<sub>2</sub> is nearly temperature-independent between 300 and 200 K. It varies as  $-\ln T$  as temperature decreases, peaks at around 20 K and then drops precipitously at lower temperatures. A distinct anomaly at 6.5 K close to the magnetic transition in this compound is noted. The  $-\ln T$  variation of the resistivity, keeping also in view the resistivity behavior of Yb<sub>2</sub>AlSi<sub>2</sub> and Yb<sub>2</sub>MgSi<sub>2</sub>, shows the presence of Kondo interaction in the mixed alloy. These results show that it is possible to track the evolution from spin fluctuating to trivalent magnetically ordered regime as x is varied from 0 to 1 in Yb<sub>2</sub>Al<sub>1-x</sub>Mg<sub>x</sub>Si<sub>2</sub>.

# 3.4. Heat capacity

The heat capacity of  $Yb_2MgSi_2$  and  $Yb_2Al_{0.5}Mg_{0.5}Si_2$  is shown in figure 7. The peak in the heat capacity clearly reflects the bulk magnetic transition at the respective  $T_N$  of the two compounds.

Since we do not have the data on non-magnetic, reference analog  $Lu_2MgSi_2$ , which would have given us a measure of the lattice heat capacity, we have estimated approximately the entropy associated with the magnetic transition by smoothly



**Figure 7.** The heat capacity of  $Yb_2MgSi_2$  and  $Yb_2Al_{0.5}Mg_{0.5}Si_2$  between 1.8 and 20 K. The inset shows the heat capacity of  $Gd_2MgSi_2$  between 1.8 and 50 K.

extrapolating the low temperature C/T data to 0 K and the C/T plot above the magnetic transition to the intercept at 0 K. Following this procedure we obtain an entropy of nearly 4 and 1.9 J/Yb mol K in Yb<sub>2</sub>MgSi<sub>2</sub> and Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub>, respectively. These values are less than *R*ln2, expected for a doublet S = 1/2 ground state, by 30% and 67% respectively in the two compounds. Reduced entropy in the magnetically ordered state often arises due to the presence of short range order above  $T_{\rm N}$ . An additional mechanism due to the partial quenching of the Yb magnetic degrees of freedom by Kondo screening may also be operative, particularly in YbAl<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub>.

The inset of figure 7 shows the heat capacity of Gd<sub>2</sub>MgSi<sub>2</sub> which orders magnetically at 31 K. De Gennes scaling predicts the magnetic ordering temperature of a Yb analog in an isostructural series of rare earth compounds to be about 1% of the Gd compound, thus suggesting a magnetic transition temperature of ~0.3 K in Yb<sub>2</sub>MgSi<sub>2</sub>. Therefore, the experimental  $T_N$  of 9.5 K implies a huge enhancement of the magnetic ordering temperature in Yb<sub>2</sub>MgSi<sub>2</sub>.

The heat capacity of Yb<sub>2</sub>AlSi<sub>2</sub> is shown in figure 8 in the form of C/T versus  $T^2$ . The inset shows the heat capacity *C* is monotonically decreasing with temperature *T* down to the lowest data point of 1.8 K in our experiment. However, the C/T plot shows an interesting upturn below about 12 K. An upturn in C/T can be observed as a precursor to a magnetic transition but, since *C* does not show any upturn down to 1.8 K, a *magnetic* origin of the upturn can safely be ruled out. Besides, the magnetization data in figure 2 show convincingly that Yb<sub>2</sub>AlSi<sub>2</sub> is a paramagnet. On the other hand, both the magnetization and resistivity suggest the presence of spin fluctuations in Yb<sub>2</sub>AlSi<sub>2</sub>. The paramagnon model [8–10] of spin fluctuations in exchangeenhanced paramagnets and nearly ferromagnetic materials predicts an additional contribution of the form  $T^3 \ln(T/T_{sf})$  to



**Figure 8.** The plot of the heat capacity C/T versus  $T^2$  of Yb<sub>2</sub>AlSi<sub>2</sub> between 1.8 and 20 K. The solid lines are a fit of equation (1) to the data (see text). The inset shows the data in the form of *C* versus *T*.

the electronic heat capacity for  $T \ll T_{sf}$ , where  $T_{sf}$  is the spin fluctuation temperature, such that the expression for the total heat capacity is given by

$$C = \gamma T + \beta T^3 + \delta T^3 \ln(T/T_{\rm sf}) \tag{1}$$

where the first two terms represent the usual electronic and lattice contributions to the heat capacity. Some of the wellknown materials in which a  $T^3 \ln(T/T_{sf})$  contribution to the heat capacity has been observed are UAl2 [11, 12], TiBe2 [13], the heavy fermion superconductor UPt<sub>3</sub> [12, 14],  $CeSi_x$  [15] The solid line in figure 8 shows that and  $Ni_3Al$  [16]. expression (1) provides a reasonably good fit to the data. The  $\gamma$  and  $T_{\rm sf}$  values obtained by fitting are 305 mJ mol<sup>-1</sup> K<sup>-2</sup> and 24.5 K, respectively. An independent estimate of  $\gamma$  based on the phenomenological Kadowaki–Woods relation  $A/\gamma^2 =$  $10^{-5} \mu\Omega$  cm, obeyed by a host of heavy fermion valence/spin fluctuating compounds [7], gives  $\gamma = 345.7 \text{ mJ mol}^{-1} \text{ K}^{-2}$ using the values of A as derived from the resistivity data. Overall, there is a fairly good correspondence between the magnetization, heat capacity and resistivity data, strengthening the inference of a  $T^3 \ln(T/T_{\rm sf})$  contribution to the heat capacity in Yb2AlSi2.

We have also fitted the expression  $C = \gamma T + \beta T^3 + D$  to the data, where *D* represents a contribution due to the magnetic clusters which is constant for  $T \gg T_A$ , where  $T_A = E_A/Sk_B$ ( $E_A$  is the average anisotropy energy of the cluster and *S* its spin) [17]. For the same fitting range as used for equation (1) above the fitting is very poor. However, for  $T \leq 10$  K, the fit is even better than that based on the paramagnon model, but the fitted value of the coefficient of the lattice heat capacity  $\beta$  is negative, which is physically untenable. We therefore discard the magnetic clusters-based fit as meaningless for Yb<sub>2</sub>AlSi<sub>2</sub>.

# 3.5. <sup>170</sup>Yb Mössbauer data

3.5.1.  $Yb_2MgSi_2$ . We have supplemented the bulk thermodynamic and transport data described above with the



**Figure 9.** The <sup>170</sup>Yb Mössbauer spectra in Yb<sub>2</sub>MgSi<sub>2</sub> at 4.2, 8 and 10 K. The red curve is the subspectrum (15% relative intensity) whose precise origin is not clear.

microscopic technique of <sup>170</sup>Yb Mössbauer spectroscopy. The technique is based on the  $\gamma$ -ray resonant absorption between the ground nuclear state, with spin  $I_g = 0$ , and the first excited state, with spin I = 2, at an energy 84.3 keV.

Mössbauer spectra in Yb<sub>2</sub>MgSi<sub>2</sub> were recorded in the temperature range 4.2–50 K (see figure 9). Below 10 K, the spectra show the presence of a magnetic hyperfine interaction and of a smaller quadrupolar hyperfine interaction; at 10 K and above, the quadrupolar interaction alone is present. These spectra show that magnetic ordering of Yb<sup>3+</sup> moments occurs below 10 K, which is in agreement with the bulk thermodynamic and transport data presented above.

In the paramagnetic phase ( $T \ge 10$  K), the spectrum is well accounted for by the quadrupolar hyperfine Hamiltonian in the excited nuclear state:

$$H_Q = \frac{eQV_{zz}}{8} \left[ I_Z^2 - \frac{I(I+1)}{3} + \frac{\eta}{6} (I_+^2 + I_-^2) \right]$$
(2)

where Q is the quadrupolar moment of the nuclear excited state, and  $V_{ZZ}$  and  $\eta$  are, respectively, the principal component and asymmetry parameter of the electric field gradient (EFG) tensor  $V_{ij}$  at the nucleus site. At 10 K, the fit of the spectrum to Hamiltonian (2) yields a quadrupolar parameter  $\alpha_Q = \frac{eQV_{zz}}{8} =$ 1.63(2) mm s<sup>-1</sup> and  $\eta \approx 0.65$ . The non-zero value of  $\eta$  is in agreement with the non-axial character of the local symmetry



Figure 10. Thermal variation of the Yb spontaneous moment in Yb<sub>2</sub>MgSi<sub>2</sub>. The red dotted line is a mean-field calculation for S = 1/2, appropriate for a Kramers doublet, with  $T_N = 9.1$  K.

(mm, i.e. two perpendicular mirror planes) at the Yb site. Due to this low symmetry, it is not possible to assess the position of the main axes of the EFG tensor. The above parameters do not change much up to 50 K.

In the magnetically ordered phase, the usual procedure is to diagonalize the whole hyperfine Hamiltonian in the main EFG axes. Then the hyperfine field has angles  $\theta$  and  $\phi$  in this frame. The total Hamiltonian is

$$H_{\rm hf} = -g_{\rm n}\mu_{\rm n}\mathbf{I}\cdot\mathbf{H}_{\rm hf} + H_Q \tag{3}$$

where  $g_n$  is the nuclear gyromagnetic factor and  $\mu_n$  is the nuclear Bohr magnetron. In principle, the quadrupolar parameters are little affected in the magnetically ordered phase with respect to the paramagnetic phase. Anyway, in the fits of the magnetic spectra, the parameter  $\alpha_Q$  was left free but  $\eta$  was kept fixed at the value 0.65. The other parameters were the magnitude and orientation of the hyperfine field. A further complication arises in the magnetically ordered phase because of the presence of a small intensity (about 15%) extra subspectrum (red line in figure 9), whose precise origin is unclear. Its hyperfine field is substantially larger than that of the majority subspectrum, which we shall consider to correspond to the main Yb<sub>2</sub>MgSi<sub>2</sub> phase. We shall postpone the discussion of this minority spectrum to the later portion of this section.

The results of the fits of the spectra in the magnetically ordered phase are summarized in figures 10 and 11. For rare earths, the hyperfine field is proportional to the magnetic moment to a good approximation. In the case of Yb<sup>3+</sup>, the constant of proportionality is:  $C = 102T/\mu_B$  [18]. Using the measured hyperfine field values, one can determine the moment values. At 4.2 K, the hyperfine field is 51(2) T, and thus the saturated spontaneous Yb moment is 0.51(0.02)  $\mu_B$ . This value is much reduced with respect to the free-ion saturated moment value of 4  $\mu_B$ ; this is a crystal field effect and it suggests that the Yb moment is directed along a hard magnetic axis as a consequence of exchange anisotropy, similar to the cases of YbNiSn [19] and YbNiBC [20]. The thermal



**Figure 11.** Thermal variation of the quadrupolar hyperfine parameter  $\alpha_Q$  (the red line is a guide for the eye); inset: the peak in the magnetic susceptibility at 9.5 K.

variation of the moment (figure 10) runs slightly above the expected mean field curve for an effective spin S = 1/2, which describes a well-isolated Kramers doublet, namely the ground state of Yb<sup>3+</sup> in the crystal electric field. The orientation of the moment in the EFG tensor frame is:  $\theta$  and  $\phi \sim 90^{\circ}$ .

The thermal variation of the  $\alpha_Q$  parameter (figure 11) is rather unexpected: it presents a peak at 8 K, very close to the magnetic transition ( $T_{\rm N} = 9.5$  K, see the inset of figure 11). Actually,  $\alpha_O$  (or  $V_{ZZ}(T)$ ) is made of two contributions: a lattice contribution representing the electric field gradient arising from the charges surrounding the Yb site and a usually dominant 4f contribution arising from the distortion of the 4f shell itself by the crystal electric field. This latter contribution can be expressed as a function of the 4f quadrupolar moment  $Q_{ZZ}^{4f} = \langle 3J_Z^2 - J(J+1) \rangle_T$ , where  $J_Z$  is the component of the total angular momentum **J**  $(J = 7/2 \text{ for } Yb^{3+})$  along the principal axis OZ of the EFG tensor, namely  $\alpha_Q^{\text{4f}} = B_Q Q_{ZZ}^{\text{4f}}$ ,  $B_Q$  being a hyperfine constant. The thermal variation of  $\alpha_Q$ is entirely due to the 4f contribution. Usually,  $\alpha_0$  suffers a small jump at the magnetic transition, as the Yb wavefunctions lose the mixing with excited states due to the presence of an exchange field. The presence of a peak near  $T_{\rm N}$  in its thermal variation may imply a strong coupling of the 4f quadrupolar moment with the magnetic moment through a magneto-elastic coupling [21]. Two other experimental features could be due to a strong magneto-elastic coupling: the 'squaredness' of the thermal variation of the moment and the high value of the Néel temperature (9.5 K) which is comparable to the highest ever recorded among Yb compounds.

3.5.2. The minority subspectrum. The minority subspectrum (15% relative intensity) visible in the magnetically ordered phase has a hyperfine field that decreases from 170 T at 4.2 K to 97 T at 9 K. Its presence is puzzling and has no clear explanation up to now. It could be a second Yb site in the Yb<sub>2</sub>MgSi<sub>2</sub> magnetic phase, appearing because of a peculiar magnetic structure. However, the small fraction (about 1/6) of the Yb ions in this site makes this hypothesis very unlikely.



Figure 12. <sup>170</sup>Yb Mössbauer spectrum of Yb<sub>2</sub>AlSi<sub>2</sub> at 1.5 K.

Another possibility could be the presence of a Yb silicate impurity phase, where the recoil-free fraction of the Yb site is much larger than that of the main Yb<sub>2</sub>MgSi<sub>2</sub> phase. This can occur if the atomic bonds in the impurity phase are much harder than in the main phase, leading to a much higher Debye temperature. Then, even a small Yb atomic fraction in the impurity phase (a few 0.1%) can lead to an approx. 10% spectral contribution. However, in our Yb<sub>2</sub>MgSi<sub>2</sub> sample, no Yb oxide or silicate could be detected by x-ray diffraction and metallography. Though the origin of the minority subspectrum is not clear, it has no bearing on the intrinsic magnetic behavior of Yb<sub>2</sub>MgSi<sub>2</sub>.

3.5.3. *Yb*<sub>2</sub>*AlSi*<sub>2</sub>. Mössbauer spectra were recorded between 1.5 and 30 K. They are pure hyperfine quadrupolar spectra (see figure 12) with an almost temperature-independent  $\alpha_Q \approx$ -0.95 mm s<sup>-1</sup> and  $\eta \approx$  0.7. Mössbauer spectra thus confirm the paramagnetic nature of Yb<sub>2</sub>AlSi<sub>2</sub>, at least down to 1.5 K, and provide additional proof about the absence of any minor (impurity) magnetically ordered phase(s) in this compound.

It is interesting to note that, even though the unit cell volume of  $Yb_2AlSi_2$  (193.4 Å<sup>3</sup>) is smaller than that of Yb<sub>2</sub>MgSi<sub>2</sub> (204.8  $Å^3$ ), the latter orders magnetically while the aluminide is paramagnetic. Typically a lower volume favors the trivalent magnetic configuration of the Yb ions as the ionic radius of Yb<sup>3+</sup> is less than that of the non-magnetic For example, YbCu<sub>2</sub>Si<sub>2</sub> is a valence fluctuating  $Yb^{2+}$ . compound but Yb ions in YbCu<sub>2</sub>Ge<sub>2</sub> with a larger lattice volume are in the divalent state. It may be noticed that both Si and Ge are nominally isovalent atoms. Evidently, the extra electron donated by Al with an outermost electronic configuration of 3s<sup>2</sup>3p<sup>1</sup> (compared to 3s<sup>2</sup> of Mg) affects the electronic band structure such that the 4f conduction electron hybridization is enhanced substantially, resulting in a paramagnetic ground state even though the cell volume decreases with increasing Al content. It appears that the hybridization between the Yb 4f and conduction electrons, determined mainly by the position of the 4f level with respect to the Fermi level, is sensitively poised in these compounds. In ambivalent Yb compounds external pressure decreases hybridization and favors a magnetic Yb<sup>3+</sup> state. For example, pressure studies on YbNiSn show that the magnetic transition

temperature  $T_c$  initially increases rapidly with  $dT_c/dP = 0.3 \text{ K kbar}^{-1}$  [22]. In the present case a decreased volume induced by pressure may tend to favor a paramagnetic behavior as a lower volume in this particular structure type favors a paramagnetic ground state as observed in Yb<sub>2</sub>AlSi<sub>2</sub>. The intermediate composition alloy Yb<sub>2</sub>Al<sub>0.5</sub>Mg<sub>0.5</sub>Si<sub>2</sub>, with a lower lattice volume compared to Yb<sub>2</sub>MgSi<sub>2</sub>, orders magnetically at a lower temperature and its resistivity shows Kondo behavior. The thermal variation of the resistivity of Yb<sub>2</sub>MgSi<sub>2</sub> indicates spin fluctuations at high temperatures though the compound orders magnetically at 9.5 K. Therefore, it would be interesting to see how these compounds respond to externally applied pressure.

The heat capacity of Yb<sub>2</sub>AlSi<sub>2</sub> shows an interesting upturn which is tentatively explained by the inclusion of a  $T^3 \ln(T/T_{sf})$  term in the electronic heat capacity. Such a contribution was predicted by the paramagnon model, first put forward to explain the absence of s-wave singlet superconductivity in Pd [8]. The paramagnon model also predicts that the spin fluctuations can be quenched by the application of a magnetic field with energy comparable to  $k_BT_{sf}$ , resulting in a reduced electronic specific heat [23–25]. In this regard, measurement of the heat capacity of Yb<sub>2</sub>AlSi<sub>2</sub> to lower temperatures and in high applied fields would be interesting. It may also be worthwhile to replace Al by Mg at low levels to find whether a quantum critical point is induced without the introduction of too much disorder in the system.

To conclude, our studies on  $Yb_2Al_{1-x}Mg_xSi_2$  (x = 0, 0.5and 1) show that the Yb 4f conduction electron hybridization varies drastically with x.  $Yb_2MgSi_2$  orders magnetically with a relatively high  $T_N$  of 9.5 K but  $Yb_2AlSi_2$  exhibits a Pauli paramagnetic ground state due to a strong Yb 4f conduction band mixing. At an intermediate composition of  $Yb_2Al_{0.5}Mg_{0.5}Si_2$  magnetic ordering and Kondo interaction co-exist.

# References

- Krahnenberg C and Mewis A 2000 Z. Anorg. Allg. Chem. 626 1448
- [2] Kraft R and Pottgen R 2005 Monatsh. Chem. 136 1707
- [3] Dhar S K, Manfrinetti P and Palenzona A 1997 J. Alloys Compounds 252 24
- [4] Yvon K, Jeitschko W and Parthe E 1977 J. Appl. Crystallogr. 10 73
- [5] Buschow K H J and van Daal H J 1972 Magnetism and magnetic materials AIP Conf. Proc. 5 1464
- [6] Mattens W C M 1980 *Thesis* Amsterdam University
- [7] Kadowaki K and Woods S B 1986 Solid State Commun. 58 507
- [8] Berk N F and Schrieffer J R 1966 Phys. Rev. Lett. 17 433
- [9] Doniach S and Engelsberg S 1966 Phys. Rev. Lett. 17 750
- [10] Rice M J 1967 Phys. Rev. **159** 153
- [11] Trainor R J, Brodsky M B and Culbert H V 1975 Phys. Rev. Lett. 34 1019
- [12] Frings P H and Franse J J M 1985 Phys. Rev. B 31 4355
- [13] Stewart G R, Smith J L and Brandt B L 1982 Phys. Rev. B 26 3783
- [14] Stewart G R, Fisk Z, Willis J O and Smith J L 1984 Phys. Rev. Lett. 52 679
- [15] Dhar S K, Gschneidner K A Jr, Lee W H, Klavins P and Shelton R N 1987 Phys. Rev. B 36 341
- [16] Dhar S K and Gschneidner K A Jr 1989 Phys. Rev. B 39 7453
- [17] Hahn A and Wohlfarth E P 1968 Helv. Phys. Acta 41 857
- [18] Bonville P, Imbert P, Jéhanno G, Gonzalez-Jimenez F and Hartmann-Boutron F 1984 Phys. Rev. B 30 3672
- Bonville P, Bellot P, Hodges J A, Imbert P, Jéhanno G, LeBras G, Hammamm J, Leylekian L, Chevrier G, Thuéry P, D'Onofro L, Hamzic A and Barthélémy A 1992 *Physica* B 182 105
- [20] Bonville P, Hodges J A, Hossain Z, Nagarajan R, Dhar S K, Gupta L C, Alleno E and Godart C 1999 Eur. Phys. J. B 11 377
- [21] Morin F and Schmitt D 1990 Ferromagnetic Materials vol 5, ed K H J Buschow and E P Wohlfarth (Amsterdam: Elsevier) p 5
- [22] Sparn G, Thompson J D and Hamzic A 1992 J. Alloys Compounds 181 197
- [23] Brinkman W F and Engelsberg S 1968 Phys. Rev. 169 417
- [24] Béal-Monod M T, Ma S-K and Fredkin D R 1968 Phys. Rev. Lett. 20 929
- [25] Béal-Monod M T and Daniel E 1983 Phys. Rev. B 27 4467